BRIEF COMMUNICATION OPEN Hydrogen bonding: a mechanism for tuning electronic and optical properties of hybrid organic–inorganic frameworks

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The field of hybrid inorganic–organic framework materials is one of the fastest growing fields in materials science because their enormous structural and chemical diversity presents great opportunities for creating many technologically relevant properties. One of the most important issues is controlling and tuning the structural, optical, thermal, mechanical and electronic properties of these complex materials by varying their chemistry, fabrication techniques and preparation conditions. Here we demonstrate that significant progress in this area may be achieved by introducing structural elements that form hydrogen bonds with the environment. Considering hybrid framework materials with different structural ordering containing protonated sulfonium cation H_3S^+ and electronegative halogen anions (I⁻, Br⁻, Cl⁻ and F⁻), we found that hydrogen bonding increases the structural stability of the material and may be used for tuning electronic states near the bandgap. We suggest that such a behaviour has a universal character and should be observed in hybrid inorganic–organic framework materials containing protonated cations. This effect may serve as a viable route for optoelectronic and photovoltaic applications.

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INTRODUCTION

In the past few years, hybrid organic-inorganic frameworks have aroused great interest due to the rich variety of their physical and chemical properties and potential application in nanotechnologies. These systems are prepared by binding multi-dentate organic molecules to multi-coordinate metal complexes and provide unlimited combinations of structures and properties, which enables to target design of materials for many applications.¹ In some cases, the binding may also be achieved and/or assisted by other mechanisms such as halogen bonding^{2,3} or hydrogen bonding.⁴ On one side, porous hybrid framework materials for applications in chemical sensing,⁵ gas storage⁶ and catalysis⁷ were developed. On the other side, there is a great interest to develop dense hybrid metal-organic systems for applications in optical and semiconductor devices and batteries.8 Some of dense hybrid frameworks such as [AmH]M $(HCOO)_3$ adopt the ABX₃ perovskite architecture (A = protonated amine, $[AmH]^+$, $B = M^{2+}$ is a divalent metal, and $X = HCOO^-$ is the formate anion) and exhibit a wide range of ferroelectric and multiferroic properties.9,10

Another class of hybrid perovskites of the composition [AmH] MX_3 ($M = Sn^{2+}, Pb^{2+}$ and $X = I^-, Br^-, CI^-$), which were known for more than two decades,¹¹ has recently attracted a great deal of interest. In particular, lead-based iodides MAPbI₃ and FAPbI₃ ($MA = CH_3NH_3^+$ and $FA = CH(NH_2)_2^+$ are methylammonium and formamidinium ions) show outstanding performance in solar cell applications and may be synthesised by straightforward processing methods such as spin-coating, dip-coating and vapour deposition techniques.^{12–14} The electrical power conversion efficiency of perovskite devices has shot up markedly and now reached 21.1%,¹⁵ which is believed to be the result of a unique combination of the orbital character of the conduction and valence band (VB) extrema, large absorption coefficient and long carrier diffusion lengths that result in low recombination rates.^{16,17}

It was also suggested that material stability and defect tolerance in these perovskites as well as in other organic–inorganic frameworks may be related to the presence of van der Waals interactions and hydrogen bonding.^{18–20} Recent quantum molecular dynamics simulations indicated that iodine atoms form hydrogen bonds with H atoms located at the nearest MA⁺ ion, i.e., charge fluctuations due to continuous formation and breakage of these bonds significantly contribute to the dielectric function of MAPbl₃.²¹

Motivated by these latest discoveries, we predict the possibility of tuning electronic properties of hybrid organic-inorganic materials and stabilising them by hydrogen bonds, or electrostatic binding of hydrogen to a nearby highly electronegative atom (N, O, F, etc). This type of bonding occurs in both inorganic (water) and organic (DNA and proteins) molecules and has an important role in determining the three-dimensional structures adopted by these molecules such as double-helical DNA structure. Many polymers (e.g., nylon) are also strengthened by hydrogen bonds in their main chains. Here we are considering several groups of hybrid organic-inorganic materials in which hydrogen bonds have a significant role in: (i) tuning the band structure of the material (e.g., the orbital character of electronic bands near the bandgap) by forming new bonds and changing hybridisation between the orbitals, and; (ii) stabilising the framework structure to be more resistant to structural transformations. The considered organic-inorganic materials are: (i) the three-dimensional (3D) tetragonal perovskite structures (β - phase) of H₃SPbX₃ (X = I⁻, Br⁻, CI⁻, F⁻) containing the sulfonium cation H₃S⁺; (ii) The structural δ -phase of the same materials containing a planar two-dimensional (2D) structure formed by PbX₆ octahedra with common edges in their equatorial planes, and; (iii) The 2D material with experimentally known RbPbF₃ structure in which Rb^+ cation is substituted by a protonated sulfonium H_3S^+ cation that forms hydrogen bonds with fluorine.



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RESULTS

We performed first-principles density functional theory-based calculations (see details in the Materials and methods section) for crystalline unit cells of the hybrid 2D and 3D organic-inorganic materials mentioned in the previous paragraph and studied the character of wave functions of the states near the bandgap. For this purpose, we projected the density of states (DOSs) onto atomic orbitals of different angular momenta (s, p and d) centred at different atoms. Figure 1 shows the tetragonal perovskite structure (β -phase) of H₃SPbI₃ (Figure 1a), the band structure of H₃SPbCl₃ (Figure 1b), and DOSs of four perovskite materials H_3SPbX_3 (X = I⁻, Br⁻, CI⁻, F⁻) projected onto different atomic species (Figure 1c-f). Analysis of the projected DOS in the vicinity of the bandgap indicates that sulfonium cation makes a significant difference in the orbital character of states near the bandgap as compared with MAPbl₃ and FAPbl₃ (Figure 2a-d). In MAPbl₃, the electronic bandgap is formed between the antibonding top of the VB originating from the Pb(6s)-I(5p) interactions and the antibonding conduction band minimum resulting from the Pb (6p)–I(5p) interactions. The MA⁺ cation does not introduce any states at the band edges (the partial contributions from C, N and H atomic orbitals at the energy interval of 5 eV below the VB maximum do not exceed 10^{-3} of the total DOS, see ref. 22 and Figure 2e), which could be the reason of high tolerance of this material to some defects.¹⁷

In the H₃SPbX₃ perovskites, the value of the bandgap (Table 1) is mainly defined by the size of the anion (the smallest for F⁻ and largest for I⁻) and its electronegativity (the lowest for I⁻ and highest for F⁻),²³ which is similar to the MAPbX₃ materials.^{24–28} However, in the H₃SPbX₃ perovskites, one could observe much higher contributions of the sulfur (S) and hydrogen (H) states in the energy range of 0.5–4 eV below the top of the VB, which means that sulfonium cation orbitals are hybridising with the halogen anion X(*p*) orbitals that provide the major contribution to the DOS in this area. This hybridisation is higher for anions with higher electronegativity (or smaller anion radius) being the largest



Figure 1. Crystal structure and electronic properties of perovskite H_3SPbX_3 materials. (a) The schematic of periodic unit cell of H_3SPbI_3 tetragonal perovskite (β -phase). Pb atoms are shown in grey, I—in purple, S—in yellow, H—in white. (b) Electronic band structure of tetragonal H_3SPbCI_3 . Zero of energy is positioned at the top of the valence band. (c-f) Density of states (total and projected at different atomic species) for β -phase of H_3SPbI_3 , H_3SPbBr_3 , H_3SPbCI_3 and H_3SPbF_3 , respectively. Black line indicates the total DOS; green, blue, red and magenta —partial contributions of halogen (X), lead (Pb), sulfur (S) and hydrogen (H), respectively.

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Figure 2. (**a**–**d**) DOS for H_3SPbX_3 (X = I, Br, CI and F) materials in β -phase projected at different atomic species and different angular momentum (*s*, *p* and *d*) orbitals. (**e**) PDOS for MAPbI₃ (shown for comparison). Red, green and blue lines indicate the contributions of *s*, *p* and *d* orbitals, respectively.

Table 1. Calculated electronic bandgaps for H_3SPbX_3 (X = I, Br, Cl and F) materials in β - and δ -phases					
Halogen atom (X)	Ι	Br	Cl	F	
Bandgap (eV) in β -phase (3D) Bandgap (eV) in δ -phase (2D)	1.73 2.49	2.06 2.88	2.50 3.44	3.78 3.76	
Abbreviations: 2D, two dimensional; 3D, three dimensional.					

for H₃SPbF₃ and lowest for H₃SPbI₃ (Figure 1c–f). The hybridised H₃S–X states form additional features at the DOS curves—one or more noticeable shoulders or even local peaks near the top of the VB. An analysis based on the projected DOS onto atomic orbitals of different angular momenta centred at different atoms (Figure 2) shows that these features are related to the hybridisation of S(3p)–H(1s)–X(p) orbitals, which increases energy distances between the upper VBs (Figure 1b).

In the structural δ -phases of H₃SPbX₃ materials that crystallise in unit cell four times larger than the perovskite unit cell, the planar 2D structure is formed by PbX₆ octahedra that share edges in their equatorial planes (Supplementary Figure S1a). We found that the qualitative behaviour of δ -modifications of these materials is very similar to the behaviour of their 3D perovskite counterparts, i.e., the δ -phase DOSs projected onto different atomic species also indicate a significant admixture of the S and H orbitals of the sulfonium ions near the top of the VB (Supplementary Figure S1). The bandgaps for the 2D δ -phase materials containing the Γ , Br⁻ and Cl⁻ ions are higher than in same materials in the 3D β -phase, whereas for H₃SPbF₃, the bandgaps are similar for both 2D and 3D phases (Table 1).

We also performed calculations for the 2D material H₃SPbF₃ that crystallises in experimentally known RbPbF₃ structure, in which Rb⁺ cations are substituted by protonated H₃S⁺ cations. The structure of this material is different from the δ -phase structures considered above—here the 2D planes consist of PbF₄ tetrahedra (instead of octahedra in the δ -phase) that have common edges (Figure 3a). We found that H₃S molecules in this framework

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also form hydrogen bonds with fluorine anions, and the electronic structure near the top of VB is similar to the two other groups of materials considered earlier—in addition to the fluorine *p*-states, there is a strong admixture of the S(3*p*) and H(1*s*) states that form two extra peaks in the DOS near the top of VB (Figure 3b). Both of these peaks are related to the formation of S–H–F bridges and are not observed in the original material with more isotropic Rb⁺ cations. Figure 3c shows that these peaks should be observed in the imaginary part of the dielectric function, $\varepsilon_2(\omega)$, at ultraviolet energies ~4.5 and 5.3 eV for any possible polarisation of the electric field (i.e., they will be also observed in polycrystalline samples and/or in unpolarised light experiments).



Figure 3. Electronic properties of H_3SPbF_3 material crystallising in the RbPbF₃ structure. (a) The schematic of H_3SPbF_3 crystal structure shown in the space filling mode. Pb atoms are shown in dark grey, F—in light grey, S—in yellow, H—in white. (b) Electronic density of states (total and projected at different atomic species) of H_3SPbF_3 , material crystallising in RbPbF₃ structure. Black line indicates the total DOS; green, blue, red and magenta—partial contributions of fluorine (F), lead (Pb), sulfur (S) and hydrogen (H). (c) Calculated imaginary part of the dielectric function (DF) for this material for three different polarisations of the electric field. Vertical blue arrows indicate interband electronic transitions from electronic states positioned near the top of VB (also indicated with blue arrows in b) to the edge of the conduction band.

DISCUSSION

All these results support the assumption that protonated sulfonium cation H₃S⁺ interacts with halogen anion, the interaction being stronger for anions with higher electronegativity (Cl⁻ and F⁻). To understand the nature of this interaction, we plotted the electron localisation function contours²⁹ for several considered materials in the vicinity of the H₃S-X complexes. In perovskite structure, the electron localisation function minimum between the H₃S complex and the iodine atom corresponds to the absence of bonding between them while an S-H-F electronic bridge is formed with fluorine (Figure 4a,b). This is a typical example of hydrogen bonding in which hydrogen atom electrostatically attracts to strongly electronegative fluorine. This hydrogen bond has some features of a covalent bond as well-it is directional and forms interatomic distances shorter than the sum of the van der Waals radii. An even stronger H-F hydrogen bond is observed in the H₃SPbF₃ material with RbPbF₃ structure (Figure 4c), which means that S-H-F bridges could be observed in



Figure 4. Electron localization function (ELF) contours of different H_3SPbX_3 materials in the vicinity of H_3S-X complexes. (**a**) ELF for H_3SPbI_3 in perovskite structure (β -phase). (**b**) ELF for H_3SPbF_3 in perovskite structure. (**c**) ELF for H_3SPbF_3 crystallising in RbPbF_3 structure.

Table 2. Calculated reaction, formation and Hull energies for H_3SPbX_3 (X = I, Br, CI, and F) materials in β - and δ -phases (in eV per cell)					
Material	Reaction energy	Formation energy	Hull energy		
	(β-phase/δ-phase)	(β-phase/δ-phase)	(β-phase/δ-phase)		
H_3SPbI_3	- 0.21/-0.18	- 0.48/ - 0.44	- 0.30/ - 0.26		
H_3SPbBr_3	- 0.16/- 0.14	- 0.63/ - 0.61	- 0.25/ - 0.23		
H_3SPbCI_3	- 0.10/- 0.08	- 0.97/ - 0.96	- 0.18/ - 0.17		
H_3SPbF_3	0.01/- 0.02	- 1.55/ - 1.58	- 0.07/ -0.28		
Reaction energies were calculated for the reactions: PbS+3HX \rightarrow H ₃ SPbX ₃ .					

many inorganic–organic frameworks containing sulfonium cations and highly electronegative halide anions.

The high S-H-F angle of 167–177° observed in all considered materials indicates that there is competition between the S-H covalent bond and hydrogen attraction to electronegative anion (Cl or F). Most likely, such a behaviour has even more universal character and could be observed in materials containing protonated cations based on atoms with electronegativity lower than nitrogen (e.g., phosphorus). The length of the N-H covalent bond (1.04 Å) is much lower than of the S–H and P–H bonds (1.34 and 1.44 Å), which is an important geometric factor explaining why protonated amines (e.g., MA and FA, for which most of the previous studies on inorganic-organic photovoltaic devices have been performed) prefer not to form hydrogen bonds with surrounding atoms even with those with high electronegativity. In sulfates and phosphates, however, this restriction is lifted, which provides an opportunity to form extra hydrogen bonds that could: (i) contribute in forming the unique structures of the network; (ii) increase their stability; and (iii) provide fine tuning of the states at the edges on the bandgap.

We also found that most of the considered hybrid inorganicorganic materials are stable. In addition to the formation energy, we calculated the reaction energy (the difference between the total energy of reaction products and reactants)³⁰ and the Hull energy (the difference in formation energies which evaluates the stability of a given compound against any linear combination of compounds that have the same averaged composition)^{31–33} for β - and δ -phases (Table 2). The results for H₃SPbK₃ (X = I, Br, CI and F) materials show that all of these energies are negative except the reaction energy for the β -phase of H₃SPbF₃ that is zero within the accuracy of the calculations.

SUMMARY

In conclusion, we demonstrate that tuning electronic properties of hybrid organic–inorganic complex materials may be achieved using protonated cations that form hydrogen bonds between the cation and surrounding octahedra. In particular, the value of the bandgap in the H_3SPbX_3 (X = I, Br, Cl and F) materials is defined by the size of the anion and the electronegativity of materials constituents that results in electrostatic interactions. Hydrogen bonding also makes these materials stable, which is promising for many applications. We suggest that such a behaviour should be observed in different hybrid inorganic–organic frameworks containing protonated cations.

The potential tunability of the states near the edges of the bandgap (VB maximum and conduction band minimum) could also provide a unique tool for developing different photovoltaic and optoelectronic devices including solar cells, light emission diodes, electrically driven lasers, nonlinear optical materials and systems, and charge storages (see review articles^{24–26,28,34} for more details). Hydrogen bonding mixes up the states of the protonated cation and the anion that gives a contribution to DOS and optical absorption spectra at specific frequencies close to the

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bandgap threshold (peaks or shoulders) that could be identified and selectively excited by laser. This could offer a new approach to different devices with promising applications in nanoelectronics, optics and data storages.

MATERIALS AND METHODS

We employ first-principles calculations to evaluate the electronic structure and estimate the stability of the proposed materials. Density functional theory calculations are performed with the projector augmented wave method as implemented in the Vienna Ab-initio Simulation Package.³⁵ All calculations were performed using spin-polarised generalised gradient approximation with the Perdew–Burke–Ernzerhof parameterisation for the exchange and correlation energy of interacting electrons.³⁶ The energy cutoff for the planewave basis set was set to 520 eV and a $8 \times 8 \times 8$ Monkhorst-Pack **k**-point mesh was employed. Long-range van der Waals interactions have been taken into account via the Tkatchenko and Scheffler scheme.³⁷ The convergence of the final forces is set to 0.01 eV/Å.

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CONTRIBUTIONS

All authors designed the research. FEM performed calculations. All participated in data analysis and writing the paper.

COMPETING INTERESTS

The authors declare no conflict of interest.

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